



Metro Domination Number of Triangular Snake Graph

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Abstract—

A Subset D of the vertex set V of the graph $G(V, E)$ is said to be a dominating set if every vertex in $V - D$ is adjacent to at least one vertex in D . The minimum cardinality of the dominating set is called the domination number $\gamma(G)$. The metro domination number is the order of a minimum dominating set which resolves as a metric set. It is denoted by $\gamma_{\rho}(TS_n)$. In this paper, we determine metro domination number of Triangular Snake graph.

Keywords— Domination number, Metric dimension, Metro domination number, Locating domination number.



I. INTRODUCTION

Every graph considered here are simple, finite, undirected and connected. A graph $G = (V, E)$ and $u, v \in V, d_G(u, v)$ is denoted as distance between u and v in G . We refer [4,6,7,8,9].

II. Definition

Definition 2.1: A set D of vertices in a graph $G (V, E)$ is said to be a dominating set of G , if every vertex in $V-D$ is adjacent to some vertex in D . The domination number $\gamma(G)$ of a graph G is the minimum cardinality of the dominating set in G

Definition 2.2: A subset $S \subseteq V$ is called resolving set if every pair of $u, v \in V$, there exist a vertex $w \in V$ such that the distance between vertices $u, v \in V$ is represented as $d(u, w) \neq d(v, w)$. A set of vertices $S \subseteq V(G)$ resolves G , then S is a resolving set of G and its minimum cardinality is a metric basis of G , and its cardinality is the metric dimension of G , and is represented by $\beta(G)$.

Definition 2.3: A dominating set D of $V(G)$ which is both dominating set as well as resolving set is called the metro dominating set of G . The minimum cardinality of a metro dominating set of G is called metro domination number of G , denoted by $\gamma_\beta(G)$.

Definition 2.4: A Triangular Snake Graph (TS_n) is obtained from the path P_n by replacing each edge of the path with a triangular C_3 .

That is, a Triangular Snake Graph (TS_n) is obtained from the path $u_1, u_2, u_3, \dots, u_n$ by joining the u_i and u_{i+1} to new a vertex v_i for $1 \leq i \leq n$. Hence every edge of a path is replace by a triangle.

Corollary 2.5: For any Triangular Snake Graph with n Triangles TS_n , the metro dimension is to for $n \leq 2$

Corollary 2.6: For any Triangular Snake Graph TS_n

$$, \gamma(TS_n) = \left\lceil \frac{n}{2} \right\rceil$$

III. Main results

Theorem: For all $n \geq 3$, $\gamma_\beta(TS_n) = \left\lceil \frac{n+2}{2} \right\rceil$

Proof: Let $u_1, u_2, u_3, \dots, u_n$ be the vertices of TS_n and let v_i be the new vertex obtained by joining u_i and u_{i+1} to form a triangle C_3 . By using Corollary 2.5 and Corollary 2.6, a metro dominating set D is also a dominating set.

$$\text{Thus } \gamma_\beta(TS_n) \leq \left\lceil \frac{n+2}{2} \right\rceil \quad (1)$$

We define D as follows

$$D = \{u_{2l-1}; l \geq 1\}, n \equiv 1(\text{mod } 2)$$

Choose D in the above case, then D is a dominating set and set $|D| = \left\lceil \frac{n+2}{2} \right\rceil$ and it also serves as a metric set.

$$\text{Thus } \gamma_\beta(TS_n) \geq \left\lceil \frac{n+2}{2} \right\rceil \quad (2)$$

From (1) and (2)

$$\gamma_\beta(TS_n) = \left\lceil \frac{n+2}{2} \right\rceil$$

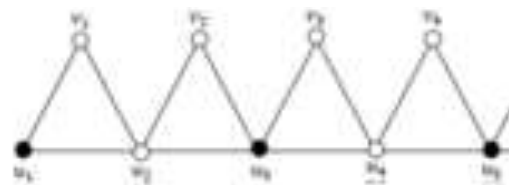


Figure 3.1: $\gamma_\beta(TS_4) = 3$



REFERENCES

- [1] S.Khuller, B.Raghavachari and A.Rosenfeld, Landmarks in graph, Discrete Appl. Math., 70(3) (1996) 217-229.
- [2] Vishukumar M, Basavaraju G.C. and Raghunath.P, Metro Domination of Square Path, Annals of Pure and Applied Mathematics Vol. 14, No. 3, 2017, 539-545 ISSN: 2279-087X (P), 2279-0888(online) Published on 19 November 2017 www.researchmathsci.org DOI: <http://dx.doi.org/10.22457/apam.v14n3a22>
- [3] Basavaraju, G. C ,On the k-metro domination number of cartesian product of $C_3 \times C_n$. International Journal of Health Sciences, 6(S9), 377823782. Retrieved from <https://sciencescholar.us/journal/index.php/ijhs/article/view/13468> (2022).
- [4]. G.C Basavaraju & Vishukumar M, On the Metro domination number of Cartesian product of path & cycle, Journal of engineering and applied sciences, 14(2019), no.1, pp.114-119.
- [5]. Slashi Leel and Sweta srivastav, Domination number in the context of some new graphs, Engineering proceedings 2024,62,14. <https://doi.org/10.3390/engproc2024062014>.
- [6]. G.C Basavaraju & Vishukumar M, On the K-Metro domination number of Cartesian product of paths, Journal of Advanced Research in Dynamical & Control System, 11(2019), no.1, pp.425-431.
- [7]. G.C Basavaraju & Rajeswari Shivaraya, Metro domination number of diamond snake graph, International Journal For Research Trends & Innovation, Vol.7, Issue-3
- [8]. G.C Basavaraju & Vishukumar M, Metro domination number of powers of path, International Journal of Emerging Technology and Advanced Engineering, 8(2017), no.3, pp.539-545.
- [9]. Vishukumar M & G.C Basavaraju, Metro domination number of square of path, Annals of Pure & Applied Mathematics, 14(2017), no.3, pp.539-545.