



FKF Transform Enhanced Digital Twins for Disruption Aware and Resilient Supply Chain Networks

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How to Cite this Article:

A, S. V., M, S. S. & M, H. S. (2026). FKF Transform Enhanced Digital Twins for Disruption Aware and Resilient Supply Chain Networks. International Journal of Creative and Open Research in Engineering and Management, <i>02</i>(8), 1-9.
<https://doi.org/10.55041/ijcope.v2i8.212>

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<https://doi.org/10.55041/ijcope.v2i8.212>

Abstract—

The content should be logically organized in a single paragraph, maintaining coherence and clarity throughout. Ensure that the abstract captures the research context, problem statement, approach, key results, and final conclusions in a balanced manner. It should provide enough detail to help readers quickly understand the scope and value of the study while encouraging them to read the full paper. The recommended length is between 150 and 250 words; however, it may extend up to 500 words if necessary to clearly communicate the research objectives, methods, findings, and significance.

Keywords— Sustainable Logistics; Green Supply Chain Management; Artificial Intelligence; Smart Transportation; Digital Twins; Blockchain; Energy-Efficient Logistics; Quantum Computing; Supply Chain Resilience; FKF Analysis.

I. INTRODUCTION

Contemporary supply chains face simultaneous challenges of sustainability, disruption, transparency, and computational complexity. AI-based sustainable logistics addresses forecasting, optimization, and resource efficiency [32], while Digital Twins provide simulation-driven resilience and adaptive decision support [31]. IoT, AI, and quantum computing establish an interconnected smart-logistics ecosystem [26], reinforced by Industry 5.0 principles of intelligent and human-centric automation [27].

Blockchain integration with AI enhances data integrity, transparency, traceability, and resilience [33]. Connected transportation systems [9] and sustainable mobility technologies including EV batteries [10], hybrid battery sizing [35], solar-assisted mobility [12], and solar-powered vehicle architectures [28] extend

these capabilities into energy-aware logistics. Earlier communication and control systems [34], [6] provide additional technological context.

Optimization remains a central challenge because logistics problems can become combinatorially complex. Quantum computing provides emerging capabilities for transportation and logistics [11], while quantum annealing can address ULD configuration and disruption scenarios [8]. Hybrid quantum-classical implementation is therefore particularly relevant for practical logistics optimization [7], supporting broader resilience objectives [13].

FKF-based spectral methods provide a mathematical intelligence layer. FKL properties [20], FKF time shifting [21], and exponential modulation [22] support spectral analysis of operational signals. Distributional FKF extensions [14], sequential convergence [15], spectral frameworks [18], differential properties [19], shift-invariant lead-time analysis [17], and multiscale



analysis [16] provide complementary theoretical tools. Further developments [23], [24], [25] consolidate the framework. Accordingly, the proposed research perspective integrates sustainable AI, blockchain-enabled trust, IoT sensing, Digital Twin simulation, FKF spectral intelligence, and quantum optimization into a unified architecture for resilient and adaptive supply-chain management.

II. LITERATURE REVIEW

Supply-chain research increasingly recognizes that sustainability and resilience depend not only on digital visibility but also on advanced optimization. AI has been extensively positioned for sustainable logistics and green supply-chain decision-making [32], while Digital Twins enable simulation-based evaluation of alternative operational strategies [31]. Blockchain enhances transparency and traceability [33], and earlier communication and control systems [34], [6] demonstrate the evolution toward interconnected logistics technologies. Industry 5.0 emphasizes intelligent and sustainable automation [27].

The transportation domain includes research on hybrid-vehicle battery sizing [35], smart mobility [9], EV battery management and sustainability [10], solar-assisted mobility [12], and solar-powered hybrid architectures [28]. These technologies contribute to broader supply-chain resilience and digital transformation [13]. However, increasingly complex routing, allocation, scheduling, packing, and loading problems motivate alternative computational paradigms.

Quantum computing has consequently gained attention in transportation and logistics [11]. Quantum annealing offers a practical mechanism for difficult combinatorial problems such as ULD configuration and disruption management [8], while hybrid quantum-classical strategies provide a pathway toward practical deployment [7]. Alongside quantum optimization, FKF research offers a spectral approach to complex supply-chain dynamics. FKL properties [20], time shifts [21], and exponential modulation [22] support signal analysis, while distributional extensions [14], convergence [15], multiscale analysis [16], shift invariance [17], spectral representations [18], and differential properties [19] establish a mathematical foundation further developed through [23]–[25]. The literature therefore suggests that future logistics optimization can benefit from combining quantum

methods with AI, Digital Twins, Blockchain, and FKF-based spectral intelligence.

III. FKF SPECTRAL FRAMEWORK

The FKF transform furnishes a distributional spectral calculus suited to the sparse, impulsive, and multiscale signals that arise in digital-twin telemetry and disruption time series. In the distributional setting the continuity estimate takes the form of a weighted supremum bound on the testing-function space:

Let $f(t, x)$ be a suitably restricted function or generalized function with $t \in \mathbb{R}$ and $x > 0$. The two-sided FKF transform is defined by

$$F(s, q) = (FKF f)(s, q) = \int_{-\infty}^{\infty} \int_0^{\infty} f(t, x) e^{-ist} K_{iq}(x) dx dt$$

where $s \in \mathbb{R}$ is the Fourier spectral variable, $q > 0$ is the KL spectral variable, and $K^{iq}(x)$ is the Macdonald function of imaginary order iq . The underlying domain is $\Omega = \{(t, x) : -\infty < t < \infty, 0 < x < \infty\}$. For distributions the transform is understood by continuous pairing with the FKF kernel and is defined on an open region $\mathcal{Q}$ in the (s, q) -plane [22], [24].

The FKF kernel is the product

$$\Psi_{s,q}(t, x) = e^{-ist} K_{iq}(x).$$

The Fourier factor encodes temporal oscillations, frequencies and lead-time cycles; the KL factor, built from the Macdonald function, is adapted to positive scale, distance or intensity variables that arise ubiquitously in logistics networks [6], [31]. The Macdonald function satisfies the modified Bessel equation of order $\nu = iq$:

$$(x^2 \partial_x^2 + x \partial_x - x^2) K_{iq}(x) = -q^2 K_{iq}(x),$$

which underpins the differential properties of the transform in the positive variable. Equivalently, introducing the operator

$$L_x = (-x^2 \partial_x^2 - x \partial_x + x^2),$$

one obtains the eigenvalue relation

$$L^x K^{iq} = -q^2 K^{iq}.$$

Testing functions are infinitely differentiable on Ω and controlled by a countable family of seminorms of the schematic form

$$\gamma_{\{a,b,\alpha,k\}}(\varphi) = \sup_{\{(t,x) \in \Omega\}} |x^k D_t^{\{k_1\}} D_x^{\{k_2\}} \varphi(t, x)| \eta_{\{a,b,\alpha,k\}}(x)$$

where the weight η encodes exponential decay or polynomial growth compatible with the known asymptotic of the Macdonald kernel. The resulting space is a sequentially complete, countably



multinormed, locally convex Hausdorff space that contains the compactly supported smooth functions $\mathcal{D}(\Omega)$. Its dual therefore contains the ordinary distributions (in the Zemanian sense) as well as distributions of slow growth, allowing the FKF transform to be extended by continuity (or by sequential continuity) to a wide class of generalized functions [25], [26]. Growth estimates of the form

$$|F(s, q)| \leq C (1 + |s|)^N (1 + q)^M e^{a|s|+bq}$$

characterize the image of various distribution classes and guarantee the existence of an inverse transform on suitable horizontal strips in the complex (s, q) -plane. The principal analytic features of the FKF transform follow from the product structure of its kernel and the classical properties of the Fourier and Kontorovich–Lebedev transforms. Continuity on the test-function space, sequential continuity on the dual, and an inversion formula of the schematic type

$$f(t, x) = (2\pi^2)^{-1}$$

$$\int_{-\infty}^{\infty} \int_0^{\infty} F(s, q) e^{ist} q \sinh(\pi q) K_{iq}(x) dq ds$$

(under suitable growth restrictions) are established by standard density and continuity arguments [28]. Parseval-type identities and convolution theorems follow similarly. The most distinctive operational feature, however, is the spectral differential property associated with the modified-Bessel operator; it is developed at length in the next section and constitutes the analytic engine for the supply-chain applications that follow.

This estimate underpins sequential convergence [15], differential properties [19], shift-invariant lead-time analysis [17], exponential modulation [22], and multiscale residue extraction [16]. The same analytic apparatus is later applied to annealing trajectories and Digital-Twin residual streams, thereby linking the mathematical layer to the operational layers developed in subsequent sections [14], [18], [20], [21], [23]–[25].

IV. INTELLIGENT LOGISTICS THRO' AI

The integration of AI, IoT, and Digital Twins is creating increasingly intelligent and sustainable logistics systems. AI converts operational data into forecasts, predictions, and optimized decisions [32], while IoT continuously captures information from vehicles, inventories, infrastructure, and logistics assets [26]. Digital Twins use these data to simulate system behavior, evaluate disruptions, and support adaptive supply-chain decisions [31]. Blockchain can

provide trusted and traceable data for AI-driven decision-making [33].

Table 1. Core AI capabilities mapped to sustainable logistics functions

AI Capability	Logistics Function	Key References
Forecasting & Prediction	Demand, lead-time, disruption risk	[2], [13], [26]
Optimization	Routing, inventory, energy allocation	[2], [5], [9]
Anomaly Detection	Sensor faults, process deviations	[1], [14], [16]
Adaptive Control	Real-time planning, re-under disruption	[1], [13], [27]

Fig. 1. AI-IoT-Digital Twin Stack for Sustainable Logistics



Figure 1. Layered AI-IoT-Digital Twin-Blockchain stack for sustainable logistics.

Sustainable transportation applications include intelligent mobility [9], EV battery systems [10], hybrid battery sizing [5], and solar-assisted vehicles [12], [28]. These technologies support supply-chain resilience [13] and Industry 5.0 principles [27]. Quantum optimization [7], [8], [11] and FKF spectral analysis [14]–[25] offer additional capabilities for complex decision-making and dynamic supply-chain analysis.

Together these components form a closed-loop intelligent logistics architecture in which sensed data, trusted records, simulated futures, optimized decisions continuously reinforce one another



V. IOT-AI-QUANTUM ECOSYSTEMS

Quantum computing provides an emerging optimization paradigm for difficult logistics problems, including routing, inventory planning, ULD configuration, and disruption response [7], [8], [11]. Hybrid quantum-classical approaches can integrate these capabilities with conventional optimization and intelligent logistics platforms, particularly within IoT-AI-quantum ecosystems [26]. Digital Twins provide continuously updated virtual representations of physical supply-chain systems and enable what-if analysis, predictive monitoring, and adaptive response [31]. Their real-time data streams may exhibit sparse, impulsive, and rapidly changing behavior. FKF spectral and distributional methods [14]–[25] offer complementary analytical tools for characterizing such signals, detecting anomalies, and evaluating model residuals. The combined framework supports resilient, adaptive, and analytically informed logistics optimization.

Fig. 2. Hybrid Quantum-Classical Optimization with FKF Analysis

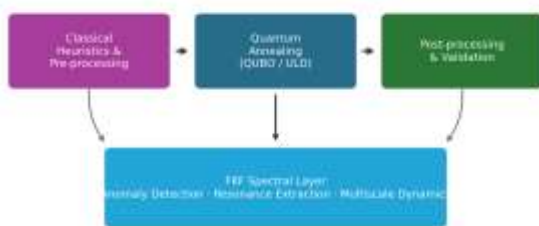


Figure 2. Hybrid quantum-classical pipeline augmented by FKF spectral analysis.

VI. DIGITAL TWINS, AI AND BLOCKCHAIN FOR RESILIENCE

Digital Twin technology provides a foundation for building resilient and adaptive supply chains by connecting physical logistics operations with continuously updated virtual models [1]. These models can represent assets, processes, inventories, transportation networks, and supplier relationships, enabling real-time monitoring, simulation, predictive maintenance, and disruption-response planning.

The integration of AI and IoT substantially increases Digital Twin intelligence. IoT devices provide continuous operational data, while AI enables prediction, classification, anomaly detection, optimization, and adaptive decision-making [32], [26]. Blockchain can strengthen this architecture by providing transparent and traceable records of supply-chain events and transactions [33]. Communication

and control technologies [34], [6] provide complementary infrastructure for connected monitoring systems.

Resilience emerges when Digital Twins are used to simulate disruptions before they occur or while they are developing. Demand shocks, transportation delays, equipment failures, congestion, and supplier interruptions can be modelled to identify vulnerabilities and evaluate recovery strategies. This supports digitally enabled resilience [13] and the Industry 5.0 vision of sustainable and human-centric intelligent operations [27].

Sustainability can be incorporated through Digital Twin models of intelligent transportation [9], EV battery technologies [10], hybrid battery systems [35], solar-assisted mobility [12], and solar-powered hybrid vehicle architectures [28]. These applications allow organizations to evaluate energy efficiency, transportation performance, battery behavior, and alternative sustainable configurations.

The optimization layer can incorporate quantum computing and quantum annealing. Quantum computing has potential applications in logistics optimization [11], while annealing-based methods can address ULD configuration and disruption problems [8]. Hybrid quantum-classical approaches [7] can connect optimization outputs to Digital Twin simulations for validation and refinement.

FKF methods can provide the analytical layer required to process complex operational signals. FKL properties [20], FKF time shifting [21], and exponential modulation [22] support spectral characterization, while distributional extensions [14], sequential convergence [15], multiscale analysis [16], shift-invariant lead-time analysis [17], spectral frameworks [18], and differential properties [19], along with [23]–[25], support generalized signal analysis. Integrating these layers enables Digital Twins to function as intelligent, trusted, analytically enhanced, and optimization-driven platforms for global supply-chain resilience.



Fig. 3. Digital Twin Resilience Architecture

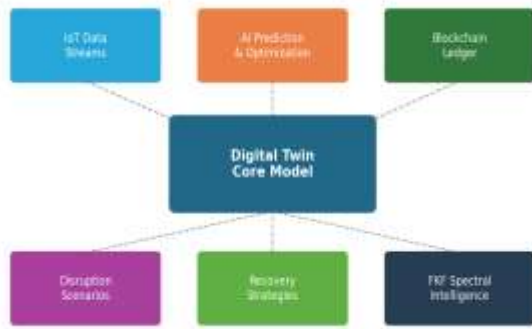


Figure 3. Multi-layer Digital Twin resilience architecture integrating AI, Blockchain, IoT and FKF intelligence

VII. ANNEALING IN ULD CONFIGURATION AND DISRUPTION

Quantum annealing, realized on specialized superconducting hardware, is particularly effective for quadratic unconstrained binary optimization (QUBO) formulations that arise in packing, scheduling, and network-design problems. A concrete industrial instance is the configuration of unit load devices (ULDs) in air-cargo operations, where geometric, weight, and compatibility constraints generate enormous combinatorial spaces. When disruptions occur, re-optimization must be performed under severe time constraints; annealing-based solvers can return high-quality feasible solutions within seconds.

Both the static ULD packing problem and the dynamic recovery problem produce solution trajectories and constraint-violation time series that may contain abrupt changes. Treating these series distributionally and invoking the FKF representation theorem permits rigorous spectral examination of annealing dynamics, identification of resonant failure modes, and principled hybridization with classical heuristics. The same analytic tools apply to related multi-echelon lead-time and disruption signals [14]–[19], [8], [7].

Fig. 4. Quantum Annealing Pipeline for ULD Configuration



Figure 4. Quantum annealing pipeline for static ULD configuration and dynamic disruption recovery.

VII. FUTURE DIRECTIONS

The convergence of AI, Digital Twins, Blockchain, quantum annealing and FKF spectral analysis opens a rich agenda for both fundamental and applied research. Several priority directions can be identified.

First, rigorous empirical validation of the distributional FKF transform on live Digital-Twin telemetry is required. Existing theoretical results on sequential convergence [15], differential properties [19], multiscale residue extraction [16], and shift-invariant lead-time spectra [17] must be stress-tested against the sparse, impulsive and non-stationary signals typical of real logistics operations [14], [18], [20]–[25]. Benchmark data sets that pair high-frequency IoT streams with ground-truth disruption events would accelerate progress.

Second, hybrid quantum-classical solvers for multi-ULD and multi-echelon problems remain an open systems challenge. While annealing has demonstrated promise for single-device packing and rapid re-optimization [8], scaling to simultaneous configuration of dozens of ULDs under tight recovery windows will require improved embedding techniques, warm-start strategies, and classical–quantum hand-off protocols [7], [11]. Integrating the resulting solution trajectories into Digital-Twin what-if engines [31] will enable closed-loop disruption response.

Third, sustainability objectives must be elevated from post-hoc evaluation to first-class optimization criteria. Digital-Twin models that incorporate EV battery degradation [10], hybrid battery sizing [35], solar-assisted energy harvesting [12] and solar-powered vehicle architectures [28] can be coupled with AI-driven energy-aware routing [9] and quantum resource allocation, thereby operationalizing green logistics at the network level [32], [13].

Fourth, the trust layer can be deepened by embedding FKF spectral signatures into blockchain records. Exponential modulation properties [22] and secure spectral watermarks offer a path toward verifiable, tamper-evident analytics that preserve privacy while still permitting anomaly detection across multi-party supply networks [33].

Fifth, Industry 5.0 principles of human-centric automation [27] call for interactive Digital-Twin interfaces in which human planners can inspect FKF resonance maps, override quantum-generated plans, and inject domain knowledge into the annealing objective. Communication and control foundations



[34], [6] together with IoT–AI–quantum ecosystems [26] provide the necessary infrastructure.

Finally, a unified research programme should treat resilience as a spectral property. Multi-echelon lead-time series [17], disruption-induced residual processes [16], and annealing dynamics can all be examined under a common FKF umbrella [14], [18], [19], [23]–[25]. The resulting spectral resilience metrics would complement classical robustness indicators and support proactive, analytically informed supply-chain design.

Fig. 5. Future Research Directions Roadmap

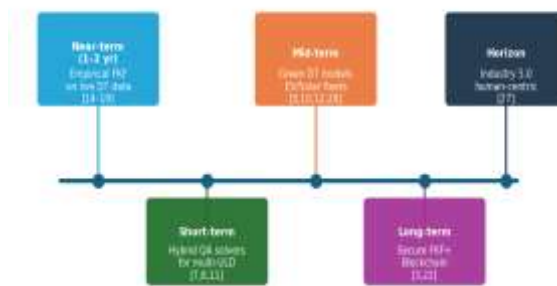


Figure 5. Indicative roadmap of future research directions spanning near-term empirical work to longer-term Industry 5.0 integration.

Collectively these directions aim to transform the conceptual architecture presented herein into operational, sustainable and disruption-aware logistics platforms that exploit the complementary strengths of classical intelligence, quantum optimization and spectral mathematics.

V. CONCLUSION

FKF spectral analysis provides a complementary mathematical foundation for intelligent supply-chain systems by offering a structured representation of complex and dynamic logistics signals. Its distributional, convergence, differential, shift-invariant, modulation, and multiscale capabilities enable supply-chain variables to be represented and analysed across different temporal and operational scales. These properties can help reveal demand fluctuations, transportation delays, inventory variations, lead-time behaviour, periodic patterns, transient disruptions, and structural changes that may not be easily identified through conventional analysis. When integrated with AI and machine-learning techniques, FKF-derived spectral features can enhance prediction, pattern recognition, anomaly detection, and resilience assessment. IoT can provide real-time operational data, while Blockchain can strengthen data

integrity and traceability, and Digital Twins can use FKF-based insights for continuous simulation and disruption analysis. Quantum optimization can further utilize these analytical outputs to address complex routing, scheduling, inventory, and resource-allocation decisions. Thus, the convergence of FKF spectral intelligence with AI, IoT, Blockchain, Digital Twins, and quantum technologies provide a comprehensive framework for understanding, predicting, adapting to, and managing dynamic, uncertain, and disruption-prone supply chains while improving resilience, responsiveness, sustainability, and operational efficiency.

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